

2)



A weight of mass  $m = 0.45 \text{ kg}$  hangs from spring of force const  $k = 15 \text{ N/m}$ .

The angular freq of oscillation is

$$\omega = \sqrt{\frac{k}{m}} = 5.77 \frac{\text{rad}}{\text{s}}$$

Fred records the motion of the system. At time  $t = 0$ , he measures

$$y(t=0) = -0.15 \text{ m}$$

$$v_y(t=0) = -1.1 \text{ m/s}$$

If we adopt

$$y(t) = A \cos(\omega t + \phi)$$

then

$$y(0) = A \cos \phi = -0.15 \text{ m}$$

$$v_y(0) = -\omega A \sin \phi = -1.1 \text{ m/s}$$

Two equations, two unknowns. Divide  $y(0)$  by  $v_y(0)$

$$\frac{A \cos \phi}{-\omega A \sin \phi} = \frac{-0.15 \text{ m}}{-1.1 \text{ m/s}}$$

$$-\frac{1}{\omega \tan \phi} = 0.136 \text{ s}$$

$$\tan \phi = -\frac{1}{(0.136 \text{ s})(5.77 \text{ rad/s})} = -1.274$$

$$\phi = -0.91 \text{ rad} + \pi \text{ rad} = +2.236 \text{ rad}$$

↑  
in proper quadrant

Then plug in to find A

$$A = \frac{-0.15 \text{ m}}{\cos(2.236 \text{ rad})} = 0.244 \text{ m}$$