

1) A piston has position given by

$$x(t) = A \cos(\omega t + \phi)$$

where

$$A = 9 \text{ m}$$

$$\omega = 0.2 \text{ rad/s}$$

$$\phi = 0.7 \text{ rad}$$

a) At time $t=5$, what is position x ?

$$\begin{aligned} x(5) &= 9 \text{ m} \cos\left(\frac{0.2 \text{ rad}}{\text{s}} * 5 \text{ s} + 0.7 \text{ rad}\right) \\ &= 9 \text{ m} \cos(1.7 \text{ rad}) \\ &= -1.16 \text{ m} \end{aligned}$$

b) The maximum speed of the piston is given by the max value of

$$v(t) = \frac{dx}{dt} = -\omega A \underbrace{\sin(\omega t + \phi)}_{\text{max of sin} = 1}$$

So.

$$\text{max } v(t) = \omega A = \left(0.2 \frac{\text{rad}}{\text{s}}\right)(9 \text{ m}) = 1.8 \text{ m/s}$$

c) How can we express position in the alternate form

$$x(t) = B \cos(\omega t) + C \sin(\omega t) \quad ?$$

Look at $x(t)$ and $v(t)$ at special time $t=0$

$$x(0) = A \cos(\phi) = B \cos(0) + C \sin(0)$$

$$\rightarrow B = A \cos(\phi) = 6.88 \text{ m}$$

$$v(0) = -\omega A \sin(\phi) = -\omega B \sin(\phi) + \omega C \cos(0)$$

$$\rightarrow C = A \sin(\phi) = -5.80 \text{ m}$$