

$$v_w - v_A = 3 \text{ m/s} \quad \Rightarrow \quad v_A = v_w - 3 \text{ m/s}$$

$$m_A v_A + m_w v_w = 0$$

$$m_A (v_w - 3 \frac{\text{m}}{\text{s}}) + m_w v_w = 0$$

$$m_A v_w - m_A 3 \frac{\text{m}}{\text{s}} + m_w v_w = 0$$

$$(m_A + m_w) v_w - m_A 3 \frac{\text{m}}{\text{s}} = 0$$

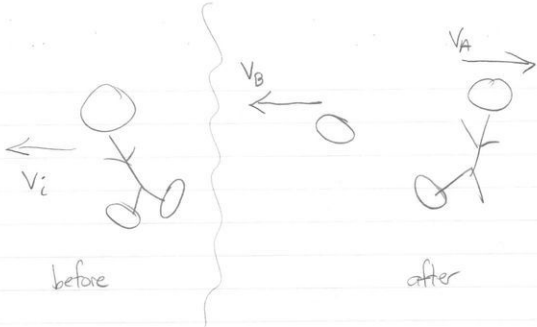
$$v_w = \frac{m_A 3 \frac{\text{m}}{\text{s}}}{(m_A + m_w)} = 2.93 \text{ m/s}$$

$$\Rightarrow v_A = 2.93 \text{ m/s} - 3 \text{ m/s} = -0.07 \text{ m/s}$$

wrench:  $x_w(t) = (+2.93 \frac{\text{m}}{\text{s}}) t$

Al  $x_A(t) = (-0.07 \frac{\text{m}}{\text{s}}) t$

cof mass  $x(t) = \emptyset$  at all times!



$$p_i = -(m_A + m_B)v_i \quad p_f = -m_B v_B + m_A v_A$$

$$v_A = \frac{-(m_A + m_B)v_i + m_B v_B}{m_A}$$

Now, we want Al to catch up to wrench in  $t \leq 1000$

$$\text{position of Al} = -0.70 \text{ m} + v_A(t - 10)$$

$$\text{position of wrench} = 0 + (2.93 \frac{\text{m}}{\text{s}})t$$

So

$$-0.70 \text{ m} + v_A(t - 10) \geq (2.93 \frac{\text{m}}{\text{s}})t \quad @ t = 1000$$

$$-0.70 \text{ m} + v_A(990) \geq (2.93 \frac{\text{m}}{\text{s}})(1000)$$

$$v_A \geq \frac{2930 \text{ m} + 0.70 \text{ m}}{990} \geq 2.96 \frac{\text{m}}{\text{s}}$$

So, use conservation of momentum to figure out the boot's speed:

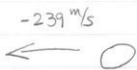
$$\text{before} \quad (Al + \text{boot}) (-0.07 \text{ m/s}) = \text{after} \quad (Al) (+2.96 \frac{\text{m}}{\text{s}}) + (\text{boot}) V_B$$

$$(m_A + m_B) (-0.07 \text{ m/s}) = m_A (2.96 \frac{\text{m}}{\text{s}}) + m_B V_B$$

$$\rightarrow V_B = \frac{(m_A + m_B) (-0.07 \frac{\text{m}}{\text{s}}) - m_A (2.96 \text{ m/s})}{m_B}$$

$$= \frac{(80 \text{ kg}) (-0.07 \frac{\text{m}}{\text{s}}) - (79 \text{ kg}) (2.96 \frac{\text{m}}{\text{s}})}{1 \text{ kg}}$$

$$= -239 \text{ m/s}$$



The relative speed of the boot and Al is

$$\boxed{\approx 242 \text{ m/s}}$$

which is how fast Al must have thrown the boot away from his hand.

Wow!