



A cart has initial velocity $\vec{v}_i = 2.40 \frac{\text{m}}{\text{s}} \hat{i}$ at $t_1 = 0.00 \text{ s}$.
It accelerates at

$$\vec{a}(t) = \left(3.45 \frac{\text{m}}{\text{s}^4} \right) t^2 \hat{i}$$

for $t_2 = 0.50$ seconds, when it reaches the end of the table.

Therefore, its speed at end of table is

$$\begin{aligned} \vec{v}(t) &= \vec{v}_i + \int_{t_1}^{t_2} \vec{a}(t) dt \\ &= 2.40 \frac{\text{m}}{\text{s}} \hat{i} + \left(3.45 \frac{\text{m}}{\text{s}^4} \right) \hat{i} \int_{t_1}^{t_2} t^2 dt \\ &= 2.40 \frac{\text{m}}{\text{s}} \hat{i} + \left(3.45 \frac{\text{m}}{\text{s}^4} \right) \hat{i} \left[\frac{1}{3} t^3 \right]_0^{0.50} \\ &= 2.40 \frac{\text{m}}{\text{s}} \hat{i} + \left(3.45 \frac{\text{m}}{\text{s}^4} \right) \hat{i} \left[\frac{1}{3} (0.50\text{s})^3 \right] \\ &= 2.40 \frac{\text{m}}{\text{s}} \hat{i} + 0.14 \frac{\text{m}}{\text{s}} \hat{i} \end{aligned}$$

$$v_f = 2.54 \frac{\text{m}}{\text{s}} \hat{i}$$

Next, we need to compute distance D it travels horizontally. It will help to know the time it spends in the air, t_{air} .

Time to fall from initial height $H = 0.75 \text{ m}$ to the ground is

$$y(t) = y_i + v_y t + \frac{1}{2} a_y t^2$$
$$= H + 0 + \frac{1}{2} (-9.8 \frac{\text{m}}{\text{s}^2}) t^2$$

At time t_{air} , cart reaches the ground, so

$$y(t_{\text{air}}) = 0 = H - 4.9 \frac{\text{m}}{\text{s}^2} \cdot t_{\text{air}}^2$$

$$\Rightarrow t_{\text{air}} = \sqrt{\frac{0.75 \text{ m}}{4.9 \frac{\text{m}}{\text{s}^2}}} = 0.391 \text{ s}$$

The cart moves as a projectile in the air, with constant x-velocity $v_x = v_f = 2.54 \frac{\text{m}}{\text{s}} \uparrow$. So

$$D = x_i + v_x t_{\text{air}} + \frac{1}{2} a_x t_{\text{air}}^2$$
$$= 0 + (2.54 \frac{\text{m}}{\text{s}} \uparrow)(0.391 \text{ s}) + 0$$

$$D = 0.995 \text{ m}$$