



a) time to complete one complete pace is period of pendulum with length L .

$$\omega = \sqrt{\frac{g}{L}}$$

$$\rightarrow \underline{P} = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{L}{g}}$$

b) during this time, animal will move forward by

$2d$ during right foot in air

$2d$ during left foot in air

$4d$ total

but $d = L \sin \theta$, so forward $4L \sin \theta$

c) Suppose $\theta = 10$ degrees. Let's compute speeds of various animals.

An adult human will travel during one full pace

$$\frac{\text{distance}}{\text{time}} = \frac{4L \sin \theta}{2\pi \sqrt{\frac{L}{g}}}$$

So speed will be

$$\begin{aligned} v &= \frac{2 \sqrt{g} \sqrt{L} \sin \theta}{\pi} \\ &= \frac{2 \sqrt{9.8 \frac{\text{m}}{\text{s}^2}} \sqrt{1 \text{m}} \sin 10^\circ}{\pi} \\ &= 0.35 \text{ m/s} \end{aligned}$$

check: adult humans walk at about 3 mph ≈ 1.3 m/s, so this formula and method doesn't seem very accurate.

Perhaps $\theta > 10^\circ$?

d) child with $L = 0.5 \text{ m} \Rightarrow v = 0.25 \text{ m/s} \approx \frac{1}{2} \text{ mph}$
slower than adult.

This does go in the right direction.

e) Allosaurus w/ $L = 2\text{m} \Rightarrow v = 0.49\text{ m/s}$

faster than adult human.

This goes in right direction.

f) In general,

$$v \propto \sqrt{L}$$

so longer legs implies faster motion.

g) human on moon. Here $L = 1\text{m}$, but $g \neq 9.8\text{ m/s}^2$.

Instead, $g_{\text{moon}} \approx 1.62\text{ m/s}^2$

$$\Rightarrow v \approx \frac{2 \sqrt{g_{\text{moon}}} \sqrt{L} \sin \theta}{\pi}$$

$\approx 0.14\text{ m/s}$ vs. 0.35 m/s on Earth

So, walk slower on planets with lower surface gravity.