

Joe stands in room, square of length $L = 15\text{ m}$. He is at
 $(x, y) = (4\text{ m}, 10\text{ m})$

Alarms ring with freq $f = 300\text{ Hz}$ and power $P = 100\text{ W}$ each.
 Room has air of temp $T = 20^\circ\text{C}$, pressure 1 atm . Thus

$$v_{\text{sound}} = 343\text{ m/s}$$

$$\rho_{\text{air}} = 1.20\text{ kg/m}^3$$

The wavelength of sound waves is

$$\lambda = \frac{v_{\text{sound}}}{f} = 1.143\text{ m}$$

alarm in corner	distance (m)	number of wavelengths	phase offset
1	6.403	5.600	216°
2	12.083	10.568	204°
3	14.866	13.002	1°
4	10.770	9.420	151°

To turn the number of wavelengths into a phase offset, use this method:

$$\text{phase} = \left(\text{fractional \# of wavelengths} \right) * 360^\circ$$

We can compute the intensity of waves from each alarm using

$$\text{Intensity} = \frac{\text{Power}}{4\pi r^2} = \frac{(\Delta P_{\text{max}})^2}{2\rho v}$$

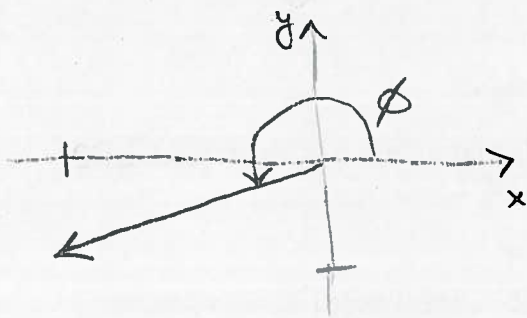
alarm in corner	distance (m)	Intensity ($\frac{W}{m^2}$)	Pressure Amplitude ($\frac{N}{m^2}$)
1	6.403	0.194	12.6
2	12.083	0.0545	6.70
3	14.866	0.0360	5.44
4	10.770	0.0686	7.51

Now that we have amplitude and phase of each wave, we can add them with phasors.

WAVE	eqn
1	$(12.6 \frac{N}{m^2}) \cos(kx - \omega t + 216^\circ)$
2	$(6.70 \frac{N}{m^2}) \cos(kx - \omega t + 204^\circ)$
3	$(5.44 \frac{N}{m^2}) \cos(kx - \omega t + 1^\circ)$
4	$(7.51 \frac{N}{m^2}) \cos(kx - \omega t + 151^\circ)$

Break each wave into components:

wave	$x = A \cos(\phi)$	$y = A \sin(\phi)$
1	$-6.57 \frac{N}{m^2}$	$-4.42 \frac{N}{m^2}$
2	-6.12	-2.73
3	$+5.44$	$+0.09$
4	$+6.57$	$+3.64$
total	-13.82	-3.42



combined wave has

$$\text{phase} = \tan^{-1}\left(\frac{-3.42}{-13.82}\right) = 194^\circ$$

$$\text{amp} = \sqrt{\left(13.82 \frac{N}{m^2}\right)^2 + \left(3.42 \frac{N}{m^2}\right)^2}$$

$$\text{amp} = 14.2 \frac{N}{m^2}$$