

Earthquake!

crust  $\rho = 3000 \text{ kg/m}^3$

wavelength  $\lambda = 430 \text{ m}$

period  $P = 0.8 \text{ s}$

amplitude  $A = 2.1 \text{ m}$

a) Displacement is

$$y(x,t) = A \cos(kx - \omega t)$$

where

$$k = \frac{2\pi}{\lambda} = 0.0146 \frac{\text{rad}}{\text{m}}$$

$$\omega = \frac{2\pi}{P} = 7.85 \frac{\text{rad}}{\text{s}}$$

b) speed of the wave is

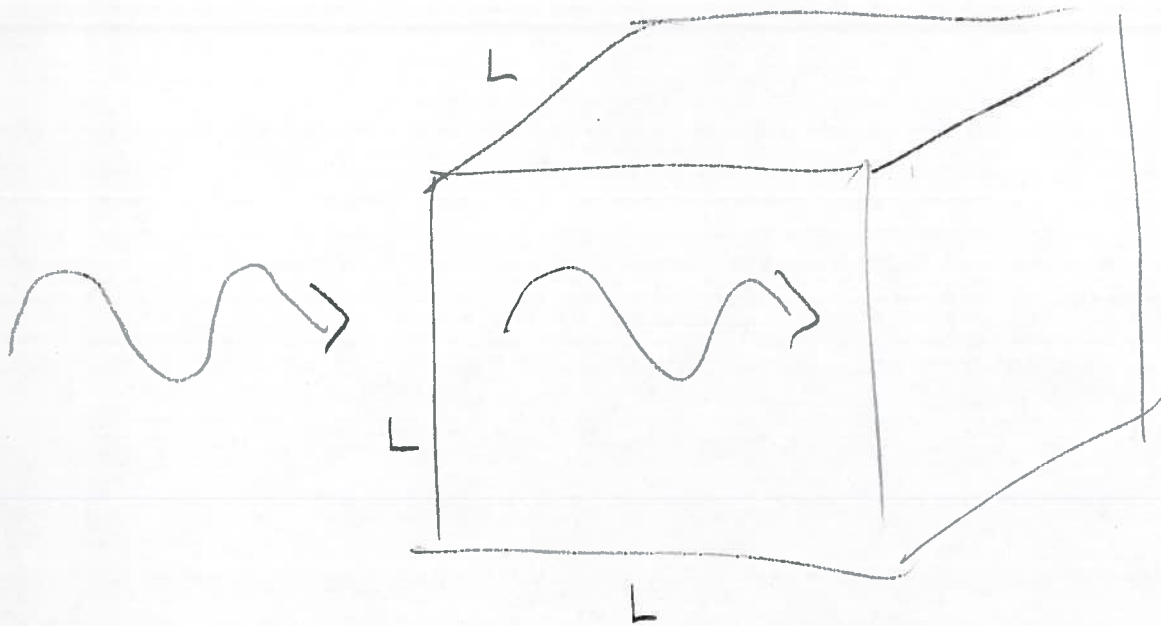
$$\text{wave speed } v = \frac{\omega}{k} = 537 \frac{\text{m}}{\text{s}}$$

c) max speed of little bits of crust as they move in response to the wave is

$$v_{\text{max}} = \left. \frac{dy}{dt} \right|_{\text{max}} = \omega A = 16.5 \frac{\text{m}}{\text{s}}$$

d) intensity of wave is

$$I = \frac{1}{2} \rho v_{\text{wave}} (\omega A)^2 = 1.35 \times 10^{10} \frac{\text{Watts}}{\text{m}^2}$$



A region of rock in the form of a cube with sides of length  $L = 100 \text{ m}$  is struck by the earthquake's wave. The wave passes through it for  $t = 6$  seconds.

The energy deposited by the wave in this region is

$$\begin{aligned} E &= (\text{Intensity}) (\text{Area of cross-section}) (\text{time}) \\ &= (1.35 \times 10^{10} \frac{\text{W}}{\text{m}^2}) (100 \text{ m})^2 (6 \text{ s}) \\ &= 8.1 \times 10^{14} \text{ J} \end{aligned}$$

This is somewhat larger than the energy released by the Hiroshima Bomb, which was  $\approx 10^{14} \text{ J}$ .