

1. The Very Large Array (VLA) is a radio interferometer consisting of 28 antennas. The VLA cycles between configurations, moving the antennas to cover different resolutions. These configurations are labeled A, B, C, and D.

- a. You want to use the VLA to observe emission in the L-band (1.5 GHz or 1.5×10^9 Hz) what wavelength are you observing? Are there any interesting lines in this band?
- b. In the table below, B_{\max} is the maximum antenna separation for each configuration.

VLA Config	B_{\max} [km]
A-array	36.4
B-array	11.1
C-array	3.4
D-array	1.03

- i. Which configuration has the highest resolution, why?
- ii. The VLA's resolution is generally diffraction limited. Use the wavelength in Part a to calculate the minimum angular scale you can observe the D-array.
- c. You're reading a paper that reports the brightness temperature of a source observed with the VLA in the L-band is 25 Kelvin. What is the intensity of the source (in units of $\text{W}/\text{m}^2/\text{Hz}/\text{sr}$ or $\text{Joules}/\text{s}/\text{m}^2/\text{Hz}/\text{sr}$)? What information do you need to determine the antenna temperature?

The Very Large Array (VLA) is a radio interferometer consisting of 28 antennas. The VLA cycles between configurations, moving the antennas to cover different resolutions. These configurations are labeled A, B, C, and D.

- d. You want to use the VLA to observe emission in the L-band (1.5 GHz or 1.5×10^9 Hz) what wavelength are you observing? Are there any interesting lines in this band?

$$\lambda = \frac{c}{f} = \frac{3e10 \frac{cm}{s}}{1.5e9} s = 20 \text{ cm}$$

This is close to the HI 21 cm line

- e. In the table below, B_{\max} is the maximum antenna separation for each configuration.

VLA Config	B_{\max} [km]
A-array	36.4
B-array	11.1
C-array	3.4
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- i. Which configuration has the highest resolution, why?

A-array is the highest resolution because it has the longest baseline.

- ii. The VLA's resolution is generally diffraction limited. Use the wavelength in Part a to calculate the minimum angular scale you can observe the D-array.

$$\theta \sim \frac{\lambda}{D} = \frac{20 \text{ cm}}{103000 \text{ cm}} = 0.00019 \text{ rad} = 40 \text{ arcseconds}$$

- f. You're reading a paper that reports the brightness temperature of a source observed with the VLA in the L-band is 25 Kelvin. What is the intensity of the source (in units of $\text{W/m}^2/\text{Hz/sr}$ or $\text{Joules/s/m}^2/\text{Hz/sr}$)? What information do you need to determine the antenna temperature?

$$\begin{aligned} \frac{2k\nu^2}{c^2} T_B &= (25 \text{ K} * 2 * 1.380649e-23 \text{ J/K} * (1.5e9)^2) / (2.99e8 \text{ m/s}) ** 2 \\ &= 1.7e-20 \text{ (J/s) / Hz/m}^2/\text{sr or W/Hz/m}^2/\text{sr} \end{aligned}$$

To determine the antenna temperature, you need the solid angle of the source and the solid angle of the beam

Bonus:

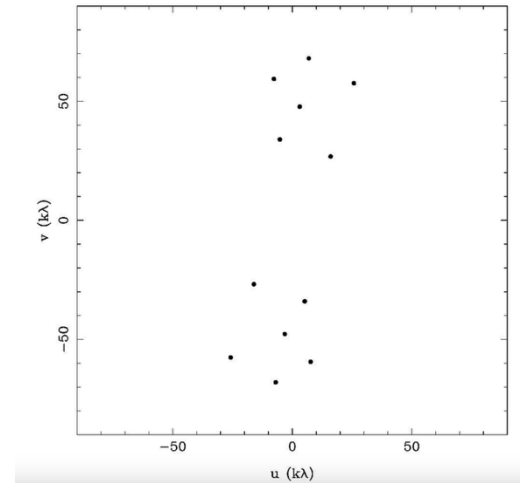
2. Using the VLA as an example, answer the following questions about interpreting the uv plane.

- a. How many antennas were used in this one sample?

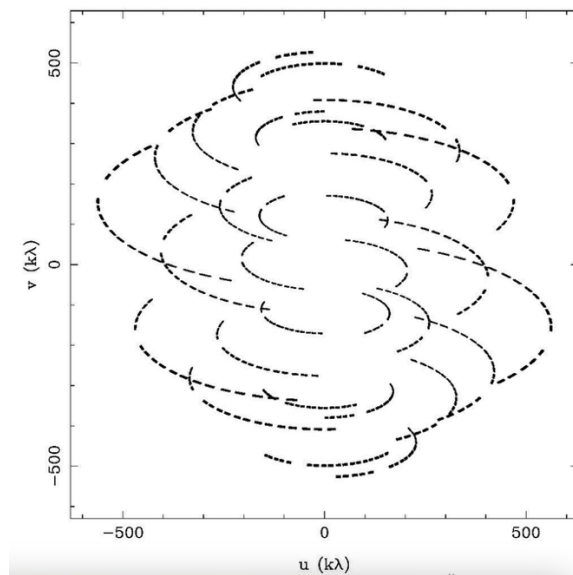
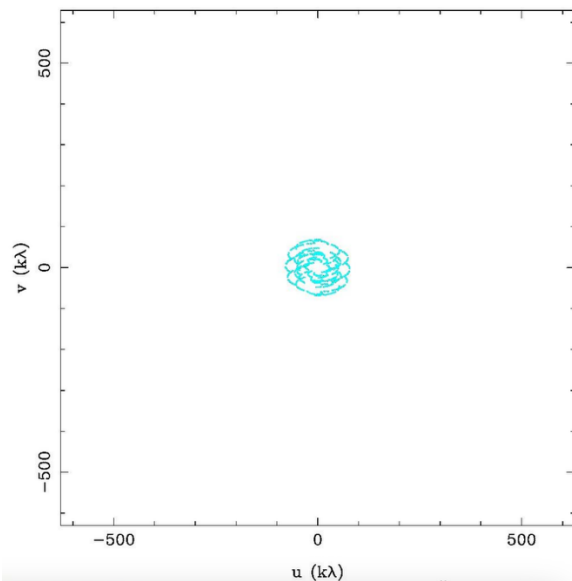
$$6 \text{ combinations} = n(n-1)/2$$

$$0 = n^2 - n - 12$$

$$(n+3)(n-4) \text{ so } n = 4$$



- b. Which one of the two samplings below is the longer baseline array? Explain.



The right is the longer baseline array because of the longer u-v distances. u and v are spatial frequencies. High spatial frequencies are due to fine structure probed by long baselines.